

ET 438a  
Continuous and Digital Control  
Integral Process Homework

A tank is drained by a pump that removes liquid at a fixed rate of  $0.027 \text{ m}^3/\text{sec}$ . The full scale flow rate of the pump is  $0.075 \text{ m}^3/\text{sec}$ . The tank has a diameter of 5 meters and is 7.5 meters high. This height is considered the full scale level that the tank can hold. The current level ( $t=0$ ) in the tank is 35% of its full scale value. The input flow rate into the tank varies due to system demand and is modeled with the following equation:

$$q_{in}(t) = 0.0097 \sin(0.25t) + 0.022 \text{ m}^3/\text{sec}$$

Assuming that  $q_{out}$  is constant find: 1.) percent  $q_{in}$  in terms of full scale pump flow, 2.) the integral time constant for the system,  $T_i$ , 3.) a function that gives the tank height as a function of time,  $h(t)$ , with the initial height of liquid level set at  $t=0$ . 4.) Find the height of liquid in the tank after 5 minutes has elapsed from  $t=0$ .