

## Three-Phase Power Measurement

### EXERCISE OBJECTIVE

When you have completed this exercise, you will be able to calculate active, reactive, and apparent power in balanced, wye- or delta-connected, three-phase circuits. You will know how to use a power meter to measure power in single-phase circuits. You will also know how to measure power in three- and four-wire, three-phase circuits.

### DISCUSSION OUTLINE

The Discussion of this exercise covers the following points:

- Calculating power in balanced three-phase circuits
- Power measurements in single-phase circuits
- Measuring the total power in four-wire, three-phase circuits
- Measuring the total power in three-wire, three-phase circuits (two-wattmeter method)
- Measuring the total power in four-wire, three-phase circuits using the two-wattmeter method

### DISCUSSION

#### Calculating power in balanced three-phase circuits

As seen in the previous exercise, the total active power  $P_T$  supplied to a balanced three-phase load (i.e., the total active power dissipated in a circuit) can be calculated using the following equation:

$$P_T = 3 \times P_{Phase} = 3 (E_{Phase} \times I_{Phase} \times \cos \varphi)$$

In a wye-connected circuit,  $E_{Phase} = E_{Line}/\sqrt{3}$  and the phase current  $I_{Phase}$  is equal to the line current  $I_{Line}$ . The above equation then becomes:

$$P_T = \frac{3}{\sqrt{3}} \times E_{Line} \times I_{Line} \times \cos \varphi$$

The  $3/\sqrt{3}$  factor can be simplified to  $\sqrt{3}$ , so that the final equation for the total active power dissipated in the wye-connected circuit is:

$$P_T = \sqrt{3} (E_{Line} \times I_{Line} \times \cos \varphi) \quad (3)$$

where  $P_T$  is the total active power dissipated in the three-phase circuit, expressed in watts (W)

In a delta-connected circuit, the same equation is obtained because the phase voltage  $E_{Phase}$  is equal to the line voltage  $E_{Line}$ , and  $I_{Phase} = I_{Line}/\sqrt{3}$ . Therefore, in either a balanced wye-connected circuit or a balanced delta-connected circuit, the total active power  $P_T$  dissipated in the three-phase circuit can be calculated using Equation (3).

Since  $(E_{Phase} \times I_{Phase} \times \cos \varphi)$  is the expression representing the active power  $P_{Phase}$  dissipated in a single phase of a three-phase circuit, it follows that the expression  $E_{Phase} \times I_{Phase}$  represents the apparent power in a single phase. The total apparent power  $S_T$  in a balanced, wye- or delta-connected, three-phase circuit can thus be calculated using the following equation:

$$S_T = 3 (E_{Phase} \times I_{Phase}) \quad (4)$$

where  $S_T$  is the total apparent power in the three-phase circuit, expressed in volt-amperes (VA)

Following the same steps used to obtain the equation for calculating the total active power  $P_T$  in three-phase circuits using the line voltage  $E_{Line}$  and the line current  $I_{Line}$ , the equation for the total apparent power  $S_T$  in a three-phase circuit can be rewritten as follows:

$$S_T = \sqrt{3} (E_{Line} \times I_{Line})$$

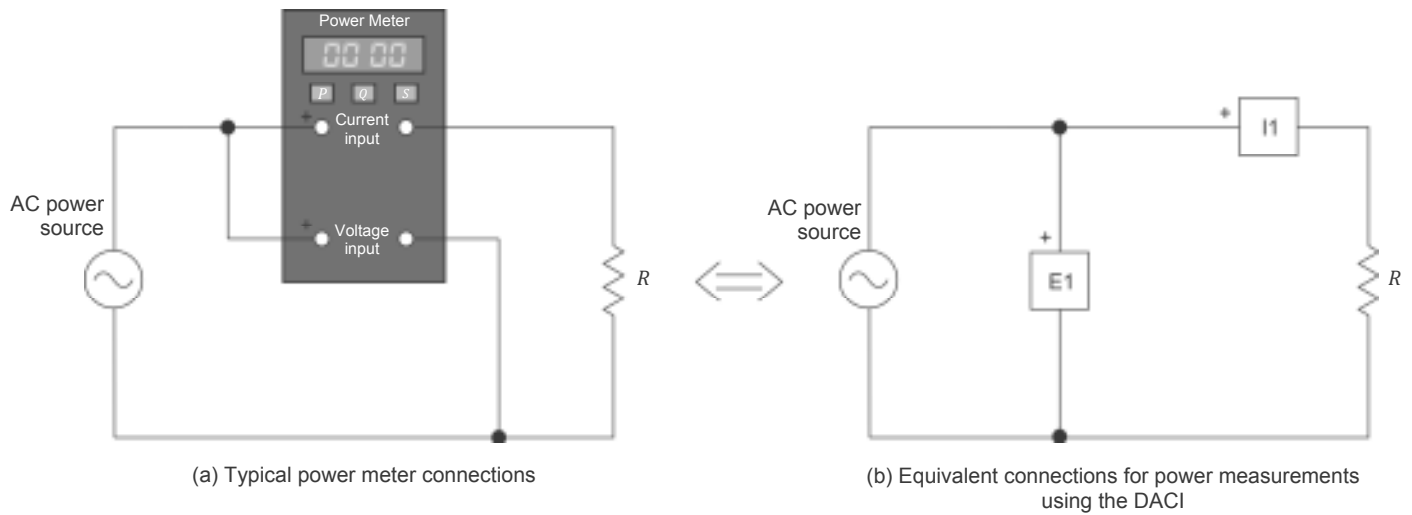
The power factor of a balanced three-phase circuit is the ratio of the total active power to the total apparent power (i.e.,  $P_T/S_T$ ), and the relationship between  $P_T$ ,  $Q_T$ , and  $S_T$  is the same as for single-phase ac circuits (i.e.,  $S_T^2 = P_T^2 + Q_T^2$ ). Thus, the total reactive power  $Q_T$  in a three-phase circuit can be calculated using the following equation:

$$Q_T = \sqrt{S_T^2 - P_T^2} \quad (5)$$

where  $Q_T$  is the total reactive power in the three-phase circuit, expressed in reactive volt-amperes (var)

### Power measurements in single-phase circuits

Commercial instruments are available to measure active, reactive, and apparent power directly. These instruments are referred to as power meters. A selector on the power meter usually allows the unit to measure active, reactive, or apparent power. A power meter determines power by measuring the circuit voltage and current. All power meters thus generally have at least a voltage input and a current input to measure the circuit voltage and current. Figure 9a shows the typical connections of a power meter in a single-phase circuit and Figure 9b shows the equivalent connections required to measure power using the Data Acquisition and Control Interface (DACI) module.



**Figure 9.** Three-phase circuit diagrams showing the connections required for power measurements.

### Measuring the total power in four-wire, three-phase circuits

Measuring the total power in a four-wire, three-phase circuit is done by first measuring the voltage and current in each phase of the circuit (i.e., the voltage across each load element and the current flowing in each load element) and calculating the active power and reactive power in each phase from the voltage and current measured in each phase of the circuit. The total active power  $P_T$  in the four-wire, three-phase circuit is simply the algebraic sum of the active power values obtained for the three phases of the circuit. Similarly, the total reactive power  $Q_T$  is simply the algebraic sum of the reactive power values obtained for the three phases of the circuit.

In other words, it is like measuring the active power and reactive power in each phase independently using three power meters and algebraically adding the three measured power (either active or reactive) values. The total apparent power  $S_T$  can then be obtained by computing the vectorial sum of the total active power  $P_T$  and the total reactive power  $Q_T$ . Figure 10 shows the connections required to measure the total power in a four-wire, three-phase circuit using the DACI. Note that, in the circuit diagram, inputs E1 and I1, inputs E2 and I2, and inputs E3 and I3 each represent a power meter.

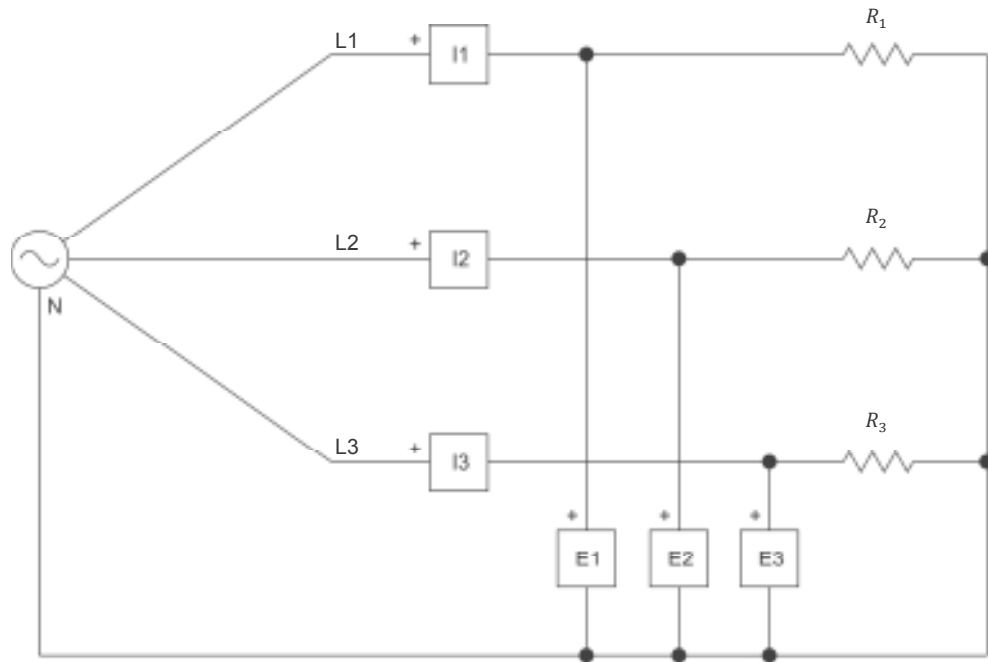


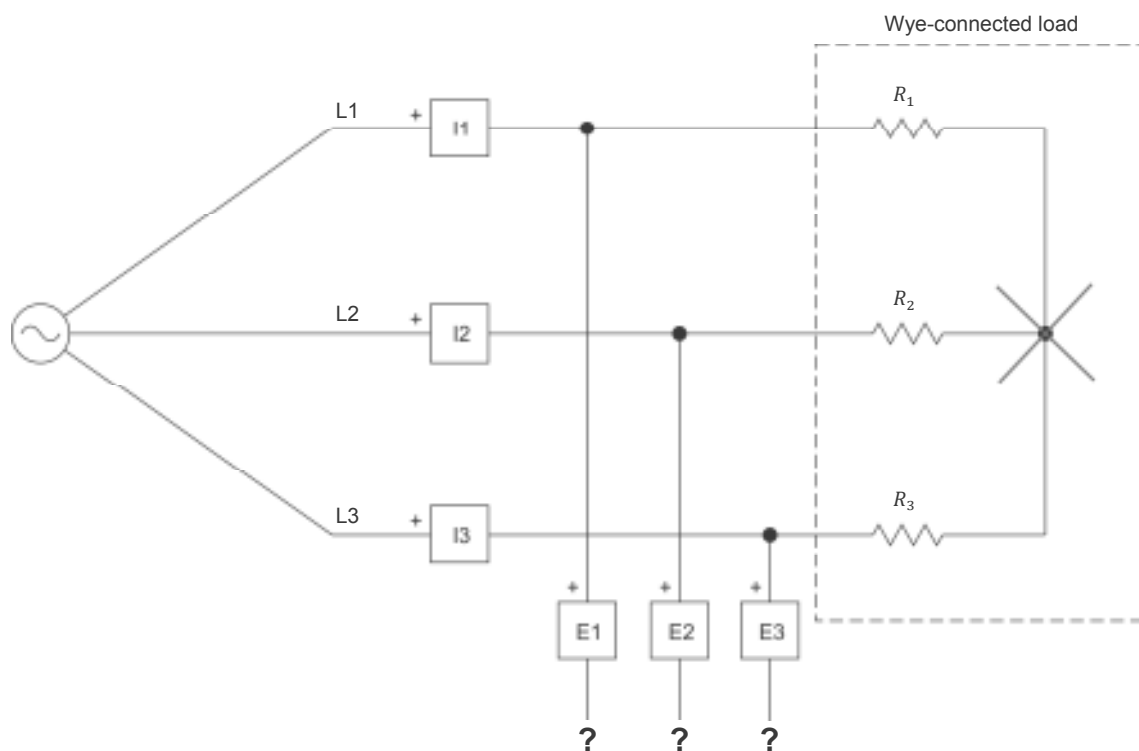
Figure 10. Three-phase power measurement using three power meters.

The method of power measurement shown in Figure 10 works whether the three-phase circuit is balanced or not.

### Measuring the total power in three-wire, three-phase circuits (two-wattmeter method)

A three-wire, three-phase circuit is simply a three-phase circuit with three line conductors but no neutral conductor. Three-wire, three-phase circuits are used commonly because they allow three-phase power to be conveyed using three conductors instead of four conductors. This makes three-wire, three-phase circuits more economical than four-wire, three-phase circuits.

The method for measuring the total power in four-wire, three-phase circuits discussed in the previous section cannot be used to measure the total power in three-wire, three-phase circuits. For instance, when the load is connected in a wye configuration, the phase currents can be measured but the phase voltages (voltage across each load element) cannot because the neutral point generally is not available to connect the voltage inputs of the power meters, as Figure 11 shows.



**Figure 11.** Diagram of a three-wire, wye-connected, three-phase circuit showing that the voltage inputs of the power meters generally cannot be connected to the neutral point of the circuit.

Similarly, when the load is connected in a delta configuration, the phase voltages can be measured but the phase currents (current flowing through each load element) cannot be measured because individual access to each load element generally is not possible (i.e., it is impossible to connect the current inputs of the power meters to measure the phase currents), as Figure 12 shows.

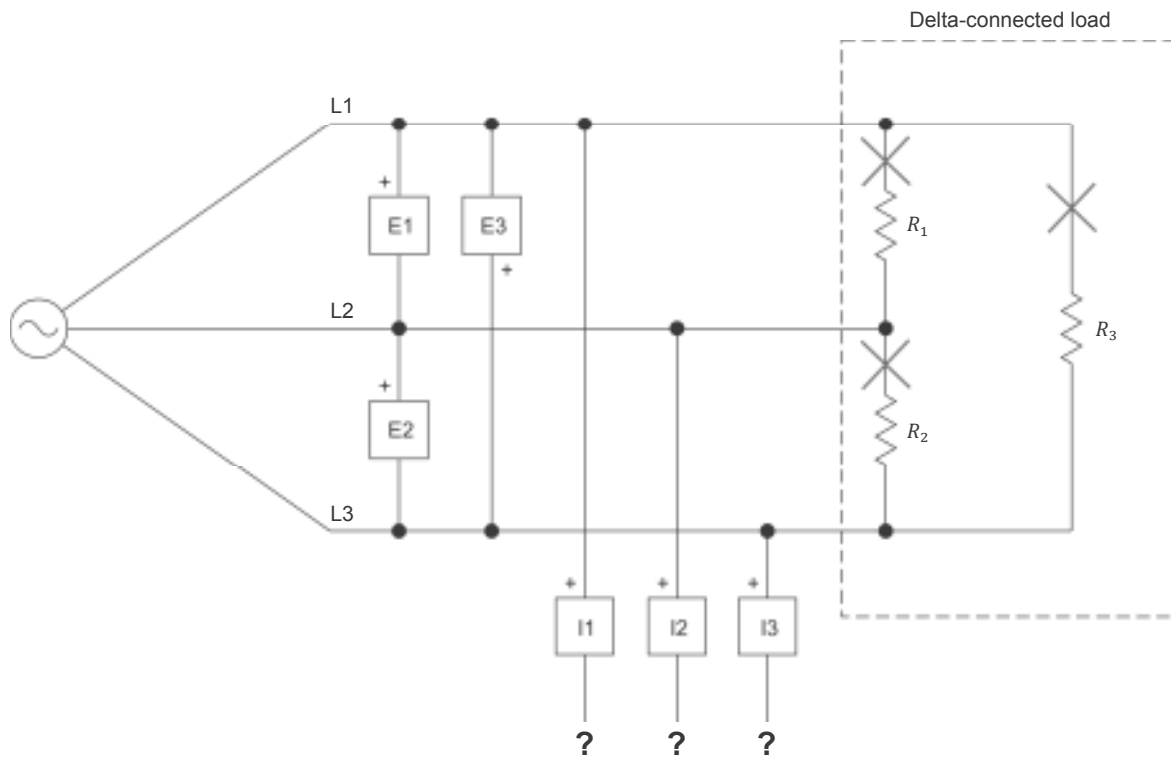


Figure 12. Diagram of a three-wire, delta-connected, three-phase circuit showing that the current inputs of the power meters cannot be connected to measure the phase currents.

To measure the total power (either the total active power  $P_T$ , the total reactive power  $Q_T$ , or the total apparent power  $S_T$ ) in three-wire, three-phase circuits, a method using only two power meters can be used. This method is usually referred to as the **two-wattmeter method** because historically, it was first implemented with two wattmeters instead of two power meters. Figure 13 shows the connections of the voltage and current inputs of the two power meters required for the two-wattmeter method of measuring three-phase power. Note that the voltage and current inputs of the power meters must be connected with the polarity indicated in the figure in order to obtain correct power measurements.

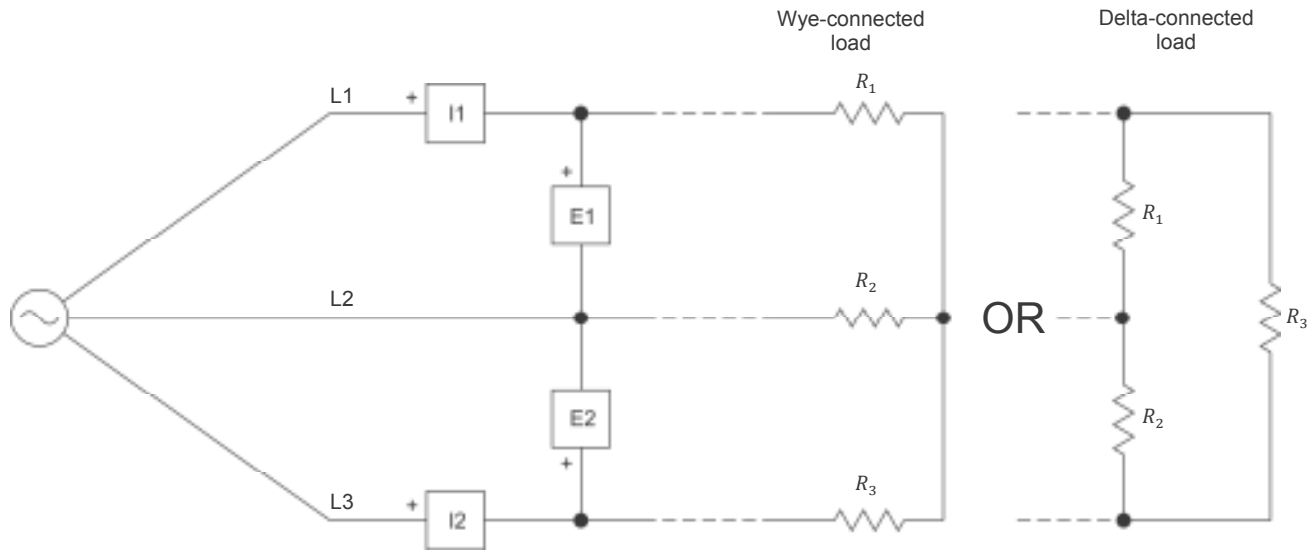


Figure 13. Connections of the voltage and current inputs of the power meters to a three-wire, three-phase circuit when measuring the total power using the two-wattmeter method.

The total active power  $P_T$  in the three-wire, three-phase circuit is simply the algebraic sum of the active power values indicated by the two power meters. Similarly, the total reactive power  $Q_T$  is simply the algebraic sum of the reactive power values indicated by the two power meters. The total apparent power  $S_T$  can then be obtained by computing the vectorial sum of the total active power  $P_T$  and the total reactive power  $Q_T$ . This method of power measurement works whether the three-phase circuit is balanced or not.

### Measuring the total power in four-wire, three-phase circuits using the two-wattmeter method

The two-wattmeter method of power measurement can also be used to measure the total power (either active, reactive, or apparent) in four-wire, three-phase circuits. This can be useful because the two-wattmeter method requires only two power meters (i.e., two voltage inputs and two current inputs) instead of three power meters (i.e., three voltage inputs and three current inputs) as with the method seen earlier in this discussion. However, care must be exercised when using the two-wattmeter method to measure the total power in four-wire, three-phase circuits because the method works only with balanced circuits.

## PROCEDURE OUTLINE

The Procedure is divided into the following sections:

- Setup and connections
- Measuring the total power in four-wire, three-phase circuits
- Measuring the total power in three-wire, three-phase circuits (wye configuration)
- Measuring the total power in three-wire, three-phase circuits (delta configuration)
- Measuring the total power in four-wire, three-phase circuits using the two-wattmeter method

## PROCEDURE



High voltages are present in this laboratory exercise. Do not make or modify any banana jack connections with the power on unless otherwise specified.

### Setup and connections

*In this section, you will set up the equipment to measure power in a four-wire, three-phase circuit.*

1. Refer to the Equipment Utilization Chart in Appendix A to obtain the list of equipment required to perform this exercise.

Install the required equipment in the Workstation.

Make sure that the ac and dc power switches on the Power Supply are set to the O (off) position, then connect the Power Supply to a three-phase ac power outlet.

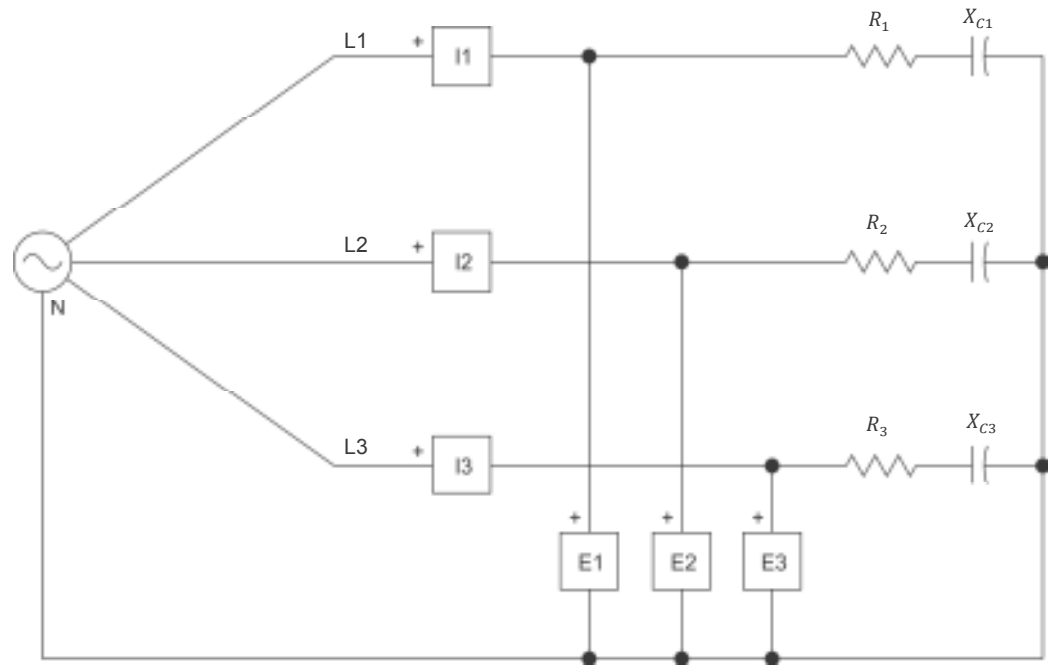
Connect the *Power Input* of the Data Acquisition and Control Interface to a 24 V ac power supply. Turn the 24 V ac power supply on.

2. Connect the USB port of the Data Acquisition and Control Interface to a USB port of the host computer.
3. Turn the host computer on, then start the LVDAC-EMS software.

In the LVDAC-EMS Start-Up window, make sure that the Data Acquisition and Control Interface is detected. Make sure that the *Computer-Based Instrumentation* function for the Data Acquisition and Control Interface is available. Select the network voltage and frequency that correspond to the voltage and frequency of your local ac power network, then click the OK button to close the LVDAC-EMS Start-Up window.



4. Set up the circuit shown in Figure 14.



Local ac power network		$R_1, R_2, R_3$ ( $\Omega$ )	$X_{C1}, X_{C2}, X_{C3}$ ( $\Omega$ )
Voltage (V)	Frequency (Hz)		
120	60	171	240
220	50	629	880
240	50	686	960
220	60	629	880

Figure 14. Balanced, four-wire, wye-connected, three-phase circuit set up for power measurements.

5. Make the necessary switch settings on the Resistive Load and Capacitive Load modules in order to obtain the resistance and capacitive reactance values required.
6. In LVDAC-EMS, start the Metering application, then make the required settings in order to measure the rms values (ac) of the phase voltages  $E_{1-N}$ ,  $E_{2-N}$ , and  $E_{3-N}$  (inputs  $E1$ ,  $E2$ , and  $E3$ , respectively), and the phase currents  $I_{Phase 1}$ ,  $I_{Phase 2}$ , and  $I_{Phase 3}$  (inputs  $I1$ ,  $I2$ , and  $I3$ , respectively). Set three other meters to measure power from inputs  $E1$  and  $I1$  (meter  $PQS1$ ),  $E2$  and  $I2$  (meter  $PQS2$ ), and  $E3$  and  $I3$  (meter  $PQS3$ ). These three power meters will be used to successively measure the active powers  $P_1$ ,  $P_2$ , and  $P_3$ , the reactive powers  $Q_1$ ,  $Q_2$ , and  $Q_3$ , and the apparent powers  $S_1$ ,  $S_2$ , and  $S_3$  in each phase of the circuit. Set the meters to continuous refresh mode.

### Measuring the total power in four-wire, three-phase circuits

*In this section, you will solve the circuit you set up in the previous section by calculating the active, reactive, and apparent power values in each phase of the circuit, and the total active, reactive, and apparent power values in the circuit. You will measure the circuit's voltage, current, and power values, and confirm that the measured circuit parameters are equal to the calculated circuit parameters. You will then unbalance the three-phase circuit by modifying the impedance in one phase of the circuit, and solve the resulting unbalanced, three-phase circuit. Finally, you will measure the total active, reactive, and apparent power values in the circuit, and verify that the measured circuit parameters are equal to the calculated circuit parameters, thus confirming that the total power in both balanced and unbalanced, four-wire, three-phase circuits can be measured using three power meters.*

7. Solve the circuit in Figure 14 to determine the following parameters: the active power  $P$ , reactive power  $Q$ , and apparent power  $S$  in each phase of the circuit, as well as the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit.

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8. Turn the three-phase ac power source in the Power Supply on.

Measure and record below the voltages and currents in the circuit of Figure 14, as well as the active power, reactive power, and apparent power in each phase of the circuit, then turn the three-phase ac power source in the Power Supply off.



*You can change the type of power (i.e., active, reactive, or apparent) measured by a power meter in the Metering window by clicking on the meter Mode button. With this method, you can rapidly perform all active power measurements, then all reactive power measurements, and finally all apparent power measurements using the same three meters.*

Voltage and current measurements:

$$E_{1-N} = \underline{\hspace{2cm}} \text{ V} \qquad I_{\text{phase } 1} = \underline{\hspace{2cm}} \text{ A}$$

$$E_{2-N} = \underline{\hspace{2cm}} \text{ V} \qquad I_{\text{phase } 2} = \underline{\hspace{2cm}} \text{ A}$$

$$E_{3-N} = \underline{\hspace{2cm}} \text{ V} \qquad I_{\text{phase } 3} = \underline{\hspace{2cm}} \text{ A}$$

Active, reactive, and apparent power measurements:

$$P_1 = \underline{\hspace{2cm}} \text{ W} \qquad P_2 = \underline{\hspace{2cm}} \text{ W}$$

$$P_3 = \underline{\hspace{2cm}} \text{ W}$$

$$Q_1 = \underline{\hspace{2cm}} \text{ var} \qquad Q_2 = \underline{\hspace{2cm}} \text{ var}$$

$$Q_3 = \underline{\hspace{2cm}} \text{ var}$$

$$S_1 = \underline{\hspace{2cm}} \text{ VA} \qquad S_2 = \underline{\hspace{2cm}} \text{ VA}$$

$$S_3 = \underline{\hspace{2cm}} \text{ VA}$$

9. Compare the voltage, current, and power (active, reactive, and apparent) values measured in the previous step with the parameter values calculated in step 7. Are all values approximately equal?

☐ Yes      ☐ No

10. In the Metering window, set an additional meter to measure the total power (either active, reactive, or apparent) from the values provided by the meters measuring the power in each phase of the circuit.



*The PQS1 + PQS2 + PQS3 function (accessible through the Meter Settings window of the Metering application) allows the sum (either algebraic or vectorial) of the power values measured by meters PQS1, PQS2, and PQS3. The total power meter can be set to indicate either the active, reactive, or apparent power value.*

11. Turn the three-phase ac power source in the Power Supply on.

Measure and record successively the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the total power meter set in the previous step, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \underline{\hspace{2cm}} \text{ W} \qquad Q_T = \underline{\hspace{2cm}} \text{ var}$$

$$S_T = \underline{\hspace{2cm}} \text{ VA}$$

Compare the total power values you just measured with the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  calculated in step 7. Are all values approximately equal?

☐ Yes      ☐ No

12. Modify the switch settings on the Resistive Load and Capacitive Load modules in the circuit of Figure 14 in order to obtain the resistance and capacitive reactance values indicated in Table 1. Due to these modifications, the three-phase load is now unbalanced (i.e., the first phase of the circuit has a different impedance from that of the second and third phases).

Table 1. Resistance and capacitive reactance values used for unbalancing the four-wire, wye-connected, three-phase circuit of of Figure 14.

Local ac power network		$R_1$ ( $\Omega$ )	$R_2, R_3$ ( $\Omega$ )	$X_{C1}$ ( $\Omega$ )	$X_{C2}, X_{C3}$ ( $\Omega$ )
Voltage (V)	Frequency (Hz)				
120	60	300	171	600	240
220	50	1100	629	2200	880
240	50	1200	686	2400	960
220	60	1100	629	2200	880

13. Solve the circuit in Figure 14 using the resistance and capacitive reactance values indicated in Table 1, to determine the following parameters: the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit.

14. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the active power  $P_T$ , reactive power  $Q_T$ , and apparent power  $S_T$  in the circuit using the total power meter you set up before, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \underline{\hspace{2cm}} \text{ W}$$

$$Q_T = \underline{\hspace{2cm}} \text{ var}$$

$$S_T = \underline{\hspace{2cm}} \text{ VA}$$

15. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  measured in the previous step with the total power values calculated in step 13. Are all values approximately equal?

☐ Yes      ☐ No

Do the circuit measurements performed in this section confirm that the total power in both balanced and unbalanced, four-wire, three-phase circuits can be measured using three power meters?

☐ Yes      ☐ No

### Measuring the total power in three-wire, three-phase circuits (wye configuration)

*In this section, you will set up a balanced, three-wire, wye-connected, three-phase circuit. You will measure the total active, reactive, and apparent power values in the circuit using the two-wattmeter method, and verify that the measured power values are equal to the calculated power values, thus confirming that the two-wattmeter method of power measurement works for measuring the total power in balanced, three-wire, three-phase circuits.*

16. Set up the circuit shown in Figure 15.



*The balanced, three-phase load in the circuit of Figure 15 is identical to the balanced, three-phase load used in the previous section of this exercise. The total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  are thus equal to those calculated in the previous section (see step 7) of the exercise.*

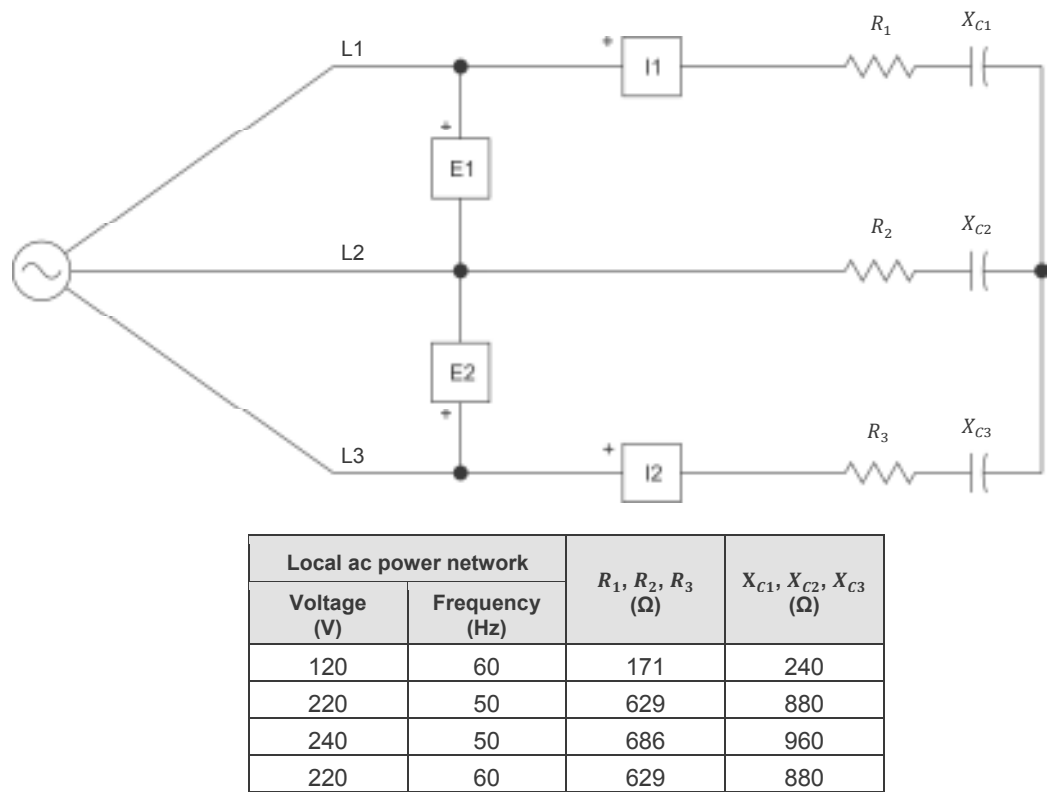


Figure 15. Balanced, three-wire, wye-connected, three-phase circuit set up for power measurements using the two-wattmeter method.

17. Make the necessary switch settings on the Resistive Load and Capacitive Load modules in order to obtain the resistance and capacitive reactance values required.
18. In the Metering window, make the required settings in order to measure the rms values (ac) of the line voltages  $E_{1-2}$  and  $E_{3-2}$  (inputs  $E1$  and  $E2$ , respectively), and the line currents  $I_{Line\ 1}$  and  $I_{Line\ 3}$  (inputs  $I1$  and  $I2$ ). Set two meters to measure power from inputs  $E1$  and  $I1$  (meter  $PQS1$ ) and inputs  $E2$  and  $I2$  (meter  $PQS2$ ). Set another meter to measure the total power from the power values provided by meters  $PQS1$  and  $PQS2$ .



The  $PQS1 + PQS2$  function (accessible through the Meter Settings window of the Metering application) allows the sum (either algebraic or vectorial) of the power values measured by meters  $PQS1$  and  $PQS2$ . The total power meter can be set to indicate either the active, reactive, or apparent power value.

19. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the meter you set up for total power measurement, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \underline{\hspace{2cm}} \text{ W}$$

$$Q_T = \underline{\hspace{2cm}} \text{ var}$$

$$S_T = \underline{\hspace{2cm}} \text{ VA}$$

20. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  measured in the previous step with the total power values calculated in step 7. Are all values approximately equal?

☐ Yes      ☐ No

Do the circuit measurements performed in this section confirm that the two-wattmeter method of power measurement can be used to measure the total power in balanced, three-wire, wye-connected, three-phase circuits?

☐ Yes      ☐ No

### Measuring the total power in three-wire, three-phase circuits (delta configuration)

*In this section, you will set up a balanced, three-wire, delta-connected, three-phase circuit. You will solve the circuit by calculating the active, reactive, and apparent power values in each phase of the circuit, and the total active, reactive, and apparent power values in the circuit. You will measure the total active, reactive, and apparent power values in the circuit using the two-wattmeter method, and confirm that the measured values are equal to the calculated values. You will then unbalance the three-phase circuit by modifying the impedance in one phase of the circuit, and solve the resulting unbalanced three-phase circuit. Finally, you will measure the total active, reactive, and apparent power values in the circuit using the two-wattmeter method, and verify that the measured values are equal to the calculated values, thus confirming that the two-wattmeter method of power measurement can be used to measure the total power in both balanced and unbalanced, three-wire, three-phase circuits.*

21. Set up the circuit shown in Figure 16.

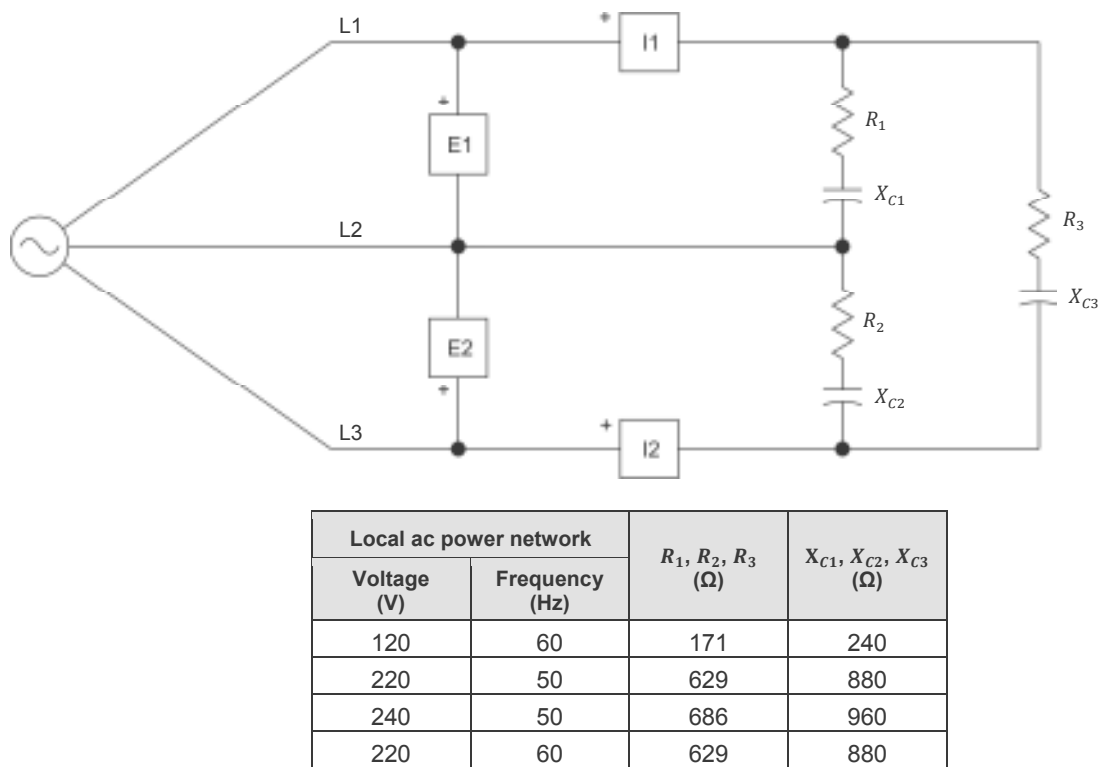


Figure 16. Balanced, three-wire, delta-connected, three-phase circuit set up for power measurements using the two-wattmeter method.

22. Make the necessary switch settings on the Resistive Load and Capacitive Load modules in order to obtain the resistance and capacitive reactance values required.
23. Solve the circuit in Figure 16 to determine the following parameters: the active power  $P$ , reactive power  $Q$ , and apparent power  $S$  in each phase of the circuit, as well as the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit.

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24. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the meter you set up for total power measurement, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \underline{\hspace{2cm}} \text{ W} \qquad Q_T = \underline{\hspace{2cm}} \text{ var}$$

$$S_T = \underline{\hspace{2cm}} \text{ VA}$$

25. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  measured in the previous step with the total power values calculated in step 23. Are all values approximately equal?

☐ Yes      ☐ No

26. Modify the switch settings on the Resistive Load and Capacitive Load modules in the circuit of Figure 16 in order to obtain the resistance and capacitive reactance values indicated in Table 2. Due to these modifications, the three-phase load is now unbalanced (i.e., the first phase of the circuit has a different impedance from that of the second and third phases).

**Table 2. Resistance and capacitive reactance values used for unbalancing the three-wire, delta-connected, three-phase circuit in Figure 16.**

Local ac power network		$R_1$ ( $\Omega$ )	$R_2, R_3$ ( $\Omega$ )	$X_{C1}$ ( $\Omega$ )	$X_{C2}, X_{C3}$ ( $\Omega$ )
Voltage (V)	Frequency (Hz)				
120	60	300	171	600	240
220	50	1100	629	2200	880
240	50	1200	686	2400	960
220	60	1100	629	2200	880

27. Solve the circuit in Figure 16 using the resistance and capacitive reactance values indicated in Table 2, to determine the following parameters: the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit.

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28. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the meter you set up for total power measurement, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \underline{\hspace{2cm}} \text{ W}$$

$$Q_T = \underline{\hspace{2cm}} \text{ var}$$

$$S_T = \underline{\hspace{2cm}} \text{ VA}$$

29. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  measured in the previous step with the total power values calculated in step 27. Are all values approximately equal?

☐ Yes      ☐ No

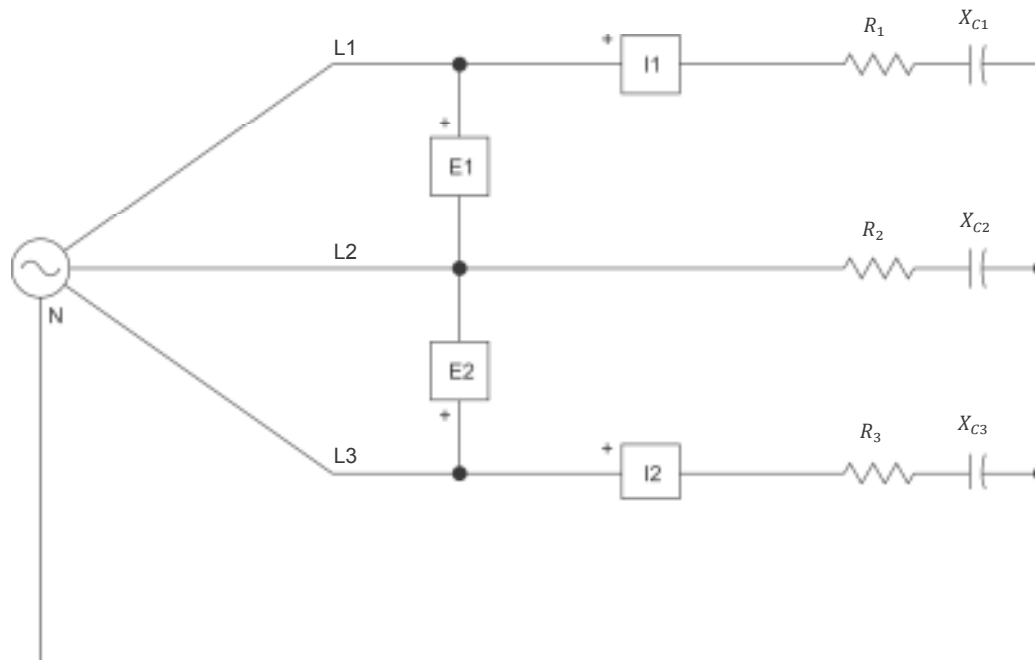
Do the circuit measurements performed in this section confirm that the two-wattmeter method of power measurement can be used to measure the total power in both balanced and unbalanced, three-wire, delta-connected, three-phase circuits?

☐ Yes      ☐ No

### Measuring the total power in four-wire, three-phase circuits using the two-wattmeter method

*In this section, you will set up a balanced, four-wire, wye-connected, three-phase circuit similar (same load but voltage and current inputs connected for total power measurement using the two-wattmeter method) to the one you set up in the “Measuring the total power in four-wire, three-phase circuits” section of this exercise. You will measure the total active, reactive, and apparent power values in the circuit using the two-wattmeter method, and confirm that the measured values are equal to the values calculated for this balanced, three-phase circuit in the “Measuring the total power in four-wire, three-phase circuits” section of this exercise. You will then unbalance the three-phase circuit by modifying the impedance in one phase of the circuit. Finally, you will measure the total active, reactive, and apparent power values in the circuit, and verify that the measured values differ from the values calculated for this unbalanced, three-phase circuit in the “Measuring the total power in four-wire, three-phase circuits” section of this exercise. You will confirm that the two-wattmeter method of power measurement can only be used to measure power in four-wire, three-phase circuits that are balanced.*

30. Set up the circuit shown in Figure 17.



Local ac power network		$R_1, R_2, R_3$ ( $\Omega$ )	$X_{C1}, X_{C2}, X_{C3}$ ( $\Omega$ )
Voltage (V)	Frequency (Hz)		
120	60	171	240
220	50	629	880
240	50	686	960
220	60	629	880

Figure 17. Four-wire, wye-connected, three-phase circuit set up for power measurements using the two-wattmeter method.

31. Make the necessary switch settings on the Resistive Load and Capacitive Load modules in order to obtain the resistance and capacitive reactance values required.



*The balanced, three-phase circuit you just set up corresponds to the balanced, four-wire three-phase circuit set up in the “Measuring the total power in four-wire, three-phase circuits” section of this exercise. The calculations required for solving the circuit are identical and do not need to be repeated.*

32. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the meter you set up for total power measurement, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \text{_____ W}$$

$$Q_T = \text{_____ var}$$

$$S_T = \text{_____ VA}$$

33. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  measured in the previous step with the total power values calculated in step 7. Are all values approximately equal?

☐ Yes      ☐ No

34. Modify the switch settings on the Resistive Load and Capacitive Load modules in the circuit of Figure 17 in order to obtain the resistance and capacitive reactance values indicated in Table 3. Due to these modifications, the three-phase load is now unbalanced (i.e., the first phase of the circuit has a different impedance from that of the second and third phases).

**Table 3. Resistance and capacitive reactance values used for unbalancing the four-wire, wye-connected, three-phase circuit.**

Local ac power network		$R_1$ ( $\Omega$ )	$R_2, R_3$ ( $\Omega$ )	$X_{C1}$ ( $\Omega$ )	$X_{C2}, X_{C3}$ ( $\Omega$ )
Voltage (V)	Frequency (Hz)				
120	60	300	171	600	240
220	50	1100	629	2200	880
240	50	1200	686	2400	960
220	60	1100	629	2200	880



*The unbalanced, three-phase circuit you just set up corresponds to the unbalanced, four-wire, three-phase circuit set up in the “Measuring the total power in four-wire, three-phase circuits” section of this exercise. The calculations required for solving the circuit are identical and do not need to be repeated.*

35. Turn the three-phase ac power source in the Power Supply on.

Successively measure and record the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  in the circuit using the meter you set up for total power measurement, then turn the three-phase ac power source in the Power Supply off.

$$P_T = \text{_____ W}$$

$$Q_T = \text{_____ var}$$

$$S_T = \text{_____ VA}$$

36. Compare the total active power  $P_T$ , total reactive power  $Q_T$ , and total apparent power  $S_T$  values measured in the previous step with the total power values calculated in step 13. Are all values equal?

☐ Yes      ☐ No

What conclusions can you draw concerning the two-wattmeter method of power measurement when measuring power in four-wire, three-phase circuits?

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37. Close LVDAC-EMS, then turn off all the equipment. Disconnect all leads and return them to their storage location.

### CONCLUSION

In this exercise, you learned how to calculate active, reactive, and apparent power in balanced, wye- and delta-connected, three-phase circuits. You also learned how to use power meters to measure power in three-phase circuits. You saw how to measure power in three- and four-wire, three-phase circuits, as well as when it is possible to use the two-wattmeter method of power measurement to measure power in a three-phase circuit.

### REVIEW QUESTIONS

1. A balanced, delta-connected, purely resistive, three-phase circuit has a line voltage  $E_{Line}$  of 100 V and a line current  $I_{Line}$  of 1.5 A. Calculate the total active power  $P_T$  dissipated in the resistive load of the circuit.

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2. Explain how to connect the two power meters to the lines of a three-wire, three-phase circuit when using the two-wattmeter method of power measurement.

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3. A balanced, wye-connected, resistive and capacitive, three-phase circuit has a phase voltage  $E_{phase}$  of 80 V and a phase current  $I_{phase}$  of 2.5 A. Calculate the total apparent power  $S_T$  in the circuit.

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4. A balanced, three-wire, resistive and capacitive, three-phase circuit is connected to two power meters set up to measure power using the two-wattmeter method of power measurement. The two power meters indicate active power readings of 175 W and -35 W. Calculate the total active power  $P_T$  dissipated in the circuit.

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5. In which type of three-phase circuits does the two-wattmeter method of power measurement not work to measure the total power in the circuit?

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